

The division of matter into three phases is not always simple. How, for example, should butter be classified? Furthermore, a fourth phase of matter can be distinguished, the **plasma** phase, which occurs only at very high temperatures and consists of ionized atoms (electrons separated from the nuclei). Some scientists believe that so-called colloids (suspensions of tiny particles in a liquid) should also be considered a separate phase of matter. **Liquid crystals**, which are used in laptop computer screens, calculators, digital watches, and so on can be considered a phase of matter intermediate between solids and liquids. However, for our present purposes we will mainly be interested in the three ordinary phases of matter.

## 10-2 Density and Specific Gravity

It is sometimes said that iron is “heavier” than wood. This cannot really be true since a large log clearly weighs more than an iron nail. What we should say is that iron is more *dense* than wood.

The **density**,  $\rho$ , of a substance ( $\rho$  is the lowercase Greek letter rho) is defined as its mass per unit volume:

$$\rho = \frac{m}{V}, \quad (10-1)$$

*Density defined*

where  $m$  is the mass of a sample of the substance and  $V$  its volume. Density is a characteristic property of any pure substance. Objects made of a particular pure substance, such as pure gold, can have any size or mass, but the density will be the same for each. (We will sometimes use the concept of density, Eq. 10-1, to write the mass of an object as  $m = \rho V$ , and the weight of an object,  $mg$ , as  $\rho Vg$ .)

The SI unit for density is  $\text{kg/m}^3$ . Sometimes densities are given in  $\text{g/cm}^3$ . Note that since  $1 \text{ kg/m}^3 = 1000 \text{ g}/(100 \text{ cm})^3 = 10^3 \text{ g}/10^6 \text{ cm}^3 = 10^{-3} \text{ g/cm}^3$ , then a density given in  $\text{g/cm}^3$  must be multiplied by 1000 to give the result in  $\text{kg/m}^3$ . Thus the density of aluminum is  $\rho = 2.70 \text{ g/cm}^3$ , which is equal to  $2700 \text{ kg/m}^3$ . The densities of a variety of substances are given in Table 10-1. The Table specifies temperature and atmospheric pressure because they affect the density of substances (although the effect is slight for liquids and solids).

**TABLE 10-1**  
**Densities of Substances<sup>†</sup>**

Substance	Density, $\rho$ ( $\text{kg/m}^3$ )
<i>Solids</i>	
Aluminum	$2.70 \times 10^3$
Iron and steel	$7.8 \times 10^3$
Copper	$8.9 \times 10^3$
Lead	$11.3 \times 10^3$
Gold	$19.3 \times 10^3$
Concrete	$2.3 \times 10^3$
Granite	$2.7 \times 10^3$
Wood (typical)	$0.3 - 0.9 \times 10^3$
Glass, common	$2.4 - 2.8 \times 10^3$
Ice ( $\text{H}_2\text{O}$ )	$0.917 \times 10^3$
Bone	$1.7 - 2.0 \times 10^3$
<i>Liquids</i>	
Water ( $4^\circ\text{C}$ )	$1.00 \times 10^3$
Blood, plasma	$1.03 \times 10^3$
Blood, whole	$1.05 \times 10^3$
Sea water	$1.025 \times 10^3$
Mercury	$13.6 \times 10^3$
Alcohol, ethyl	$0.79 \times 10^3$
Gasoline	$0.68 \times 10^3$
<i>Gases</i>	
Air	1.29
Helium	0.179
Carbon dioxide	1.98
Water (steam) ( $100^\circ\text{C}$ )	0.598

<sup>†</sup>Densities are given at  $0^\circ\text{C}$  and 1 atm pressure unless otherwise specified.

**EXAMPLE 10-1** **Mass, given volume and density.** What is the mass of a solid iron wrecking ball of radius 18 cm?

**APPROACH** First we use the standard formula  $V = \frac{4}{3}\pi r^3$  (see inside rear cover) to obtain the volume of the sphere. Then Eq. 10-1 and Table 10-1 give us the mass  $m$ .

**SOLUTION** The volume of the sphere is

$$V = \frac{4}{3}\pi r^3 = \frac{4}{3}(3.14)(0.18 \text{ m})^3 = 0.024 \text{ m}^3.$$

From Table 10-1, the density of iron is  $\rho = 7800 \text{ kg/m}^3$ , so Eq. 10-1 gives

$$m = \rho V = (7800 \text{ kg/m}^3)(0.024 \text{ m}^3) = 190 \text{ kg}.$$

The **specific gravity** of a substance is defined as the ratio of the density of that substance to the density of water at  $4.0^\circ\text{C}$ . Because specific gravity (abbreviated SG) is a ratio, it is a simple number without dimensions or units. The density of water is  $1.00 \text{ g/cm}^3 = 1.00 \times 10^3 \text{ kg/m}^3$ , so the specific gravity of any substance will be equal numerically to its density specified in  $\text{g/cm}^3$ , or  $10^{-3}$  times its density specified in  $\text{kg/m}^3$ . For example (see Table 10-1), the specific gravity of lead is 11.3, and that of alcohol is 0.79.

The concepts of density and specific gravity are especially helpful in the study of fluids because we are not always dealing with a fixed volume or mass.