

**RESPONSE** The single long vertical rod in Fig. 9–27a exerts an upward force equal to  $mg$  on pin A to support the mass  $m$  of the upper bridge. Why? Because the pin is in equilibrium, and the other force that balances this is the downward force  $mg$  exerted on it by the upper bridge (Fig. 9–27c). There is thus a shear stress on the pin because the rod pulls up on one end of the pin, and the bridge pulls down on the other end. The situation when two shorter rods support the bridges (Fig. 9–27b) is shown in Fig. 9–27d, in which only the connections at the upper bridge are shown. The lower rod exerts a force of  $mg$  downward on the lower of the two pins because it supports the lower bridge. The upper rod exerts a force of  $2mg$  on the upper pin (pin A) because the upper rod supports both bridges. Thus we see that when the builders substituted two shorter rods for each single long one, the stress in the supporting pin A was *doubled*. What perhaps seemed like a simple substitution did, in fact, lead to a tragic collapse in 1981 with a loss of life of over 100 people (see Fig. 9–1). Having a feel for physics, and being able to make simple calculations based on physics, can have a great effect, literally, on people's lives.

## \* 9–7 Spanning a Space: Arches and Domes

There are a great many areas where the arts and humanities overlap the sciences, and this is especially clear in architecture, where the forces in the materials that make up a structure need to be understood to avoid excessive deformation and collapse. Many of the features we admire in the architecture of the past were introduced not simply for their decorative effect, but for technical reasons. One example is the development of methods to span a space, from the simple beam to arches and domes.

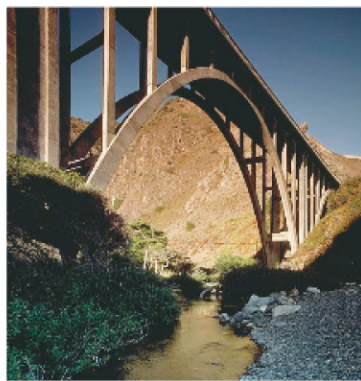
The first important architectural invention was the post-and-beam (or post-and-lintel) construction, in which two upright posts support a horizontal beam. Before steel was introduced in the nineteenth century, the length of a beam was quite limited because the strongest building materials were then stone and brick. Hence the width of a span was limited by the size of available stones. Equally important, stone and brick, though strong under compression—are very weak under tension and shear; all three types of stress occur in a beam (see Fig. 9–25). The minimal space that could be spanned using stone is shown by the closely spaced columns of the great Greek temples (Fig. 9–21).

The introduction of the semicircular **arch** by the Romans (Fig. 9–28), aside from its aesthetic appeal, was a tremendous technological innovation.

 **PHYSICS APPLIED**  
*Architecture: beams, arches  
and domes*



(a)



(b)

**FIGURE 9–28** (a) 2000-year-old round arches in Rome. The one in the background is the Arch of Titus. (b) A modern arch used to span a chasm on the California coast.